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# AS and A-level MATHS

## Forces 2

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**Specification content coverage: R4**

In this test you will be assessed on using Newton's 3rd Law, including pulleys and connected particles.

The test comprises two sections. The questions in section A will test you on the basics of the topic. Those in section B require a bit more thinking.

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**Section A: The basics**

1 Three forces  $\mathbf{A} = 2\mathbf{i} + 4\mathbf{j}$ ,  $\mathbf{B} = 6\mathbf{i} - 14\mathbf{j}$  and  $\mathbf{C} = 3\mathbf{i} + 2\mathbf{j}$  act on a particle.

1 (a) Calculate the resultant of these three forces, giving your answer in terms of  $\mathbf{i}$  and  $\mathbf{j}$ .

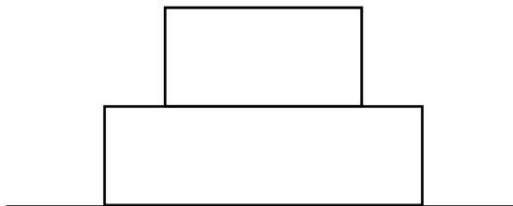
[1 mark]

1 (b) A fourth force,  $\mathbf{D}$ , acts on the particle so it remains in equilibrium.  
Find  $\mathbf{D}$ , giving your answer in terms of  $\mathbf{i}$  and  $\mathbf{j}$ .

[1 mark]

2 (a) **In this question use  $g = 10 \text{ m s}^{-2}$ .**

A box of mass 5 kg is placed on top of another box of mass 7 kg on horizontal ground, as shown in the diagram.



Draw a diagram to show the directions and magnitudes of the forces that are acting on the box of mass 5 kg.

[1 mark]

2 (b) Draw a diagram to show the directions and magnitudes of the forces that are acting on the box of mass 7 kg.

[2 marks]

3 (a) **In this question use  $g = 9.8 \text{ m s}^{-2}$ .**

A person of mass 70 kg stands on the floor of a lift.

Calculate the force exerted on the person by the floor of the lift when the lift is accelerating upwards at  $4 \text{ m s}^{-1}$ .

[2 marks]

3 (b) Calculate the force exerted on the person by the floor of the lift when the lift is accelerating downwards at  $6 \text{ m s}^{-1}$ .

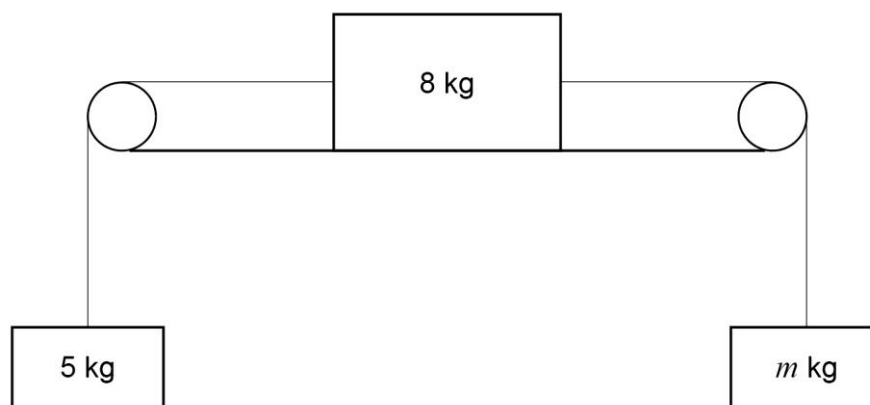
[2 marks]

4 (a) In this question use  $g = 9.8 \text{ m s}^{-2}$ .

A box of mass 8 kg rests on a smooth horizontal table.

Two strings of equal length are attached to each end of the box, and these pass over a smooth pulley at each end of the table.

The other ends of the strings are attached to other boxes, one of mass 5 kg, the other of mass  $m$  kg as shown in the diagram.



The system is released from rest and the 8 kg box moves to the left with acceleration  $1.96 \text{ m s}^{-2}$ .

By resolving vertically on the 5 kg box, find the value of the tension in the string on the left.

[2 marks]

4 (b) By resolving horizontally on the 8 kg box, find the value of the tension in the string on the right.

[2 marks]

4 (c) By resolving vertically on the  $m$  kg box, find the value of  $m$ .

[2 marks]

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**Section B: A bit more thinking**

- 5 Two trucks of masses  $3m$  kg and  $4m$  kg are pulled along a straight horizontal track by an engine of mass  $5m$  kg with a driving force of 18 550 N, as shown in the diagram.



The  $3m$  kg mass experiences a resistance of 100 N, the  $4m$  kg mass experiences a resistance of 150 N and the  $5m$  kg mass experiences a resistance of 300 N.

The system accelerates at  $2.5 \text{ m s}^{-2}$ .

Calculate the value of  $m$ , find the tension in the horizontal coupling between the trucks, and find the tension in the horizontal coupling between the  $4m$  kg truck and the engine.

- 5 (a) Calculate the value of  $m$ .

**[2 marks]**

- 5 (b) Find the tension in the horizontal coupling between the trucks and between the  $4m$  kg truck and the engine.

**[3 marks]**

- 6 **In this question use  $g = 9.8 \text{ m s}^{-2}$ .**

A box of mass 9 kg rests on a smooth horizontal table.

A string attached to the box passes over a smooth pulley at the edge of the table. The other end of the string is attached to box of mass 3 kg, which hangs vertically. The system is released from rest.

Calculate the acceleration of the system, the tension in the string and the time it takes the boxes to move 3 m.

**[6 marks]**

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**In this question use  $g = 9.81 \text{ m s}^{-2}$ .**

Two small particles of masses 6 kg and 3 kg are attached to the ends of a light inextensible string. The string passes over a smooth pulley at a height of 5 m above the ground.

The system is released from rest with both particles hanging vertically at a height of 2 m above the ground.

Explain whether the 3 kg particle will reach the pulley before it begins to move.

Fully justify your answer.

**[6 marks]**